

Energy & QoS in Systems & Networks

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2020 ICT Carbon 🔶 **1.43BTONNES** CO,

2007 ICT = **0.83BTONNES** CO₂ ~ Aviation = 2% Growth 4%

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IT footprints Emissions by sub-sector, 2020

PCs, peripherals and printers infrastructure 57% and devices 25% mate Group source: Data

Telecoms

Total emissions: 1.43bn tonnes CO₂ equivalent

360m tons CO₂

260m tons CO₂

EU 2012 \rightarrow ICT = 4.7% of Electricity Worldwide

D8.1: Overview of ICT energy consumption



Figure 3-1: Worldwide use phase electricity consumption of communication networks, personal computers and data centers. Their combined share in the total worldwide electricity consumption has grown from about 4% in 2007 to 4.7% in 2012.

Computing Loads are Generally Low



Energy Consumption at Low Loads Remains High

"The Case for Energy-Proportional Computing," Luiz André Barroso, Urs Hölzle, *IEEE Computer* December 2007



Energy Efficiency = Machine Utilization/Power

Energy Proportional Computing

"The Case for Energy-Proportional Computing," Luiz André Barroso, Urs Hölzle, *IEEE Computer* December 2007



Energy Efficiency = Server Utilization/Power Imperial College

Is this Socially Acceptable & Sustainable? **Estimated Added Value of ICT** 5~7% = CO2 Savings/ ICT CO2 Emissions Google ... and Other Myths - 0.3Wh per « Google search » - Facebook: 500Wh / User / Year - Energy Costs \$ can be as High as 15% of ICT **Operational Costs** - US Costs are 40% Less than UK and 70% Less than Germany (Canada ?) Mobile and Intermittent Computing ?? Load Averaging in Space and Time?? **Re-Use Heat ?? New Wireless Business Model?? Imperial College** Iondon

Our Work on Energy and ICT

- Energy Aware Ad Hoc Networks (2004)
- Wired Network test-bed to seek way forward (2009)
- Wired Energy-Aware Software Defined Network (2010-11)
- QoS-Energy Aware routing algorithms (2010-12)
- Energy and Time Trade-Offs in Internet Search (2010-13)
- Energy-QoS Trade-Offs in Servers and Clouds (2010-13)
- Micro & Nano-Scale (2013-2016)
- EU Projects: EU FP7 Fit4Green, ERA-NET ECROPS ...

Wireless: EPSRC ECROPS Project (2013-2016)



Effective Transmission Time VS Power P $_{T}$

Number of Bits Correctly Transmitted per Units of Power

$$\overline{D(P_T)} = \frac{f\left(\frac{rP_T}{B+\alpha P_T}\right)}{P_E + P_T}.$$

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D_{ef f}

Energy Efficiency and Computer SystemsIdeal: Power Proportional to Utilisation

 $\Pi = \omega \rho$

energy consumption per job in joules

$$J_{job} = \Pi/\lambda = \omega E[S]$$

Reality is Different

 $\Pi = A + B\rho \qquad J_{job} = \frac{A}{\lambda} + BE[S]$

Power for Compute-Intensive Apps



Power in Network Intensive HTTP



Simple Composite Cost C_{Job} for Delay and Energy • Composite Cost Function: a.[Average Response Time per Job] + b.[Average Energy Consumption per Job]

$$C_{job} = \frac{aE[S]}{1 - \lambda E[S]} + bJ_{job}$$
$$= \frac{aE[S]}{1 - \lambda E[S]} + \frac{bA}{\lambda} + bBE[S]$$

Measurements

To validate the energy-QoS metric and optimum load model, we conducted a series of experiments using jobs executing on a server class system having a quad-core Intel Xeon 3430 (8M cache, 2.4 GHz), 2 GB RAM, single 150 GB SATA hard drive, and 2 on-board Gigabit Ethernet interfaces. The system runs Linux (Ubuntu) with CPU throttling enabled with the ondemand governor, which dynamically adjust the cores' frequency depending on load. A client machine is attached to the server through a fast Ethernet switch to generate the workload, and the client machine also measures the system's power consumption [].

We measured power consumption when it is idle, i.e. when it has no external jobs to execute, to be A = 69.5 Watts, which corresponds to the value of A in equation (4).

Imperial College London Then we measured the average energy consumed by a single job from observations obtained from serving a large number of jobs (1000), the average power consumption and the total running time of the experiment. The value of B was measured to be 13.24 Watts per job on average. The measured value of J_{job} and the calculated results from (4) we the experimentally estimated values of A and B are shown



Validation Average Energy Consumption per Job vs Load



Optimisation of the Load Optimum Load that Minimises the Composite Cost



Theory versus Experimental Data



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Optimum Load Sharing among N Heterogenous Systems • Cost Function

$$C_{job} = \sum_{i=1}^{N} p_i \{ \frac{aE[S_i]}{1 - \lambda_i E[S_i]} + bJ_{job}^i \}$$
$$= \sum_{i=1}^{N} p_i \{ \frac{aE[S_i]}{1 - \lambda_i E[S_i]} + \frac{bA_i}{\lambda_i} + bB_i E[S_i] \}$$

Optimum Load Sharing

l - 1

$$\rho_{i} = 1 - \sqrt{\frac{a\sigma_{i}}{\frac{a\sigma_{i}}{(1 - \rho_{1})^{2}} + b[B_{1}\sigma_{i} - B_{i}]}}$$

where $\sigma_i = E[S_1]/E[S_i]$ is the speed-up factor Imperial College London



On-Off System

F is the ON probability, f is the On-Off rate, γ
 is the On-Off Energy Consumption

$$C_{job} = \frac{aE[S]}{F - \lambda E[S]} + b\frac{FA + \gamma f}{\lambda} + bB\frac{E[S]}{F}$$

Optimum Load is Given by

$$\rho^* = \frac{\sqrt{\frac{b(FA+\gamma f)}{a}}}{1+\sqrt{\frac{b(FA+\gamma f)}{a}}}$$



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Figure 7. Measured and theoretical average response time versus load, for the system with ON-OFFs with f = 0.005.



A=69.5, B=13.32, E[S]=5.7754 s, y=5.268 KJ

Figure 10. Theoretical and measured energy consumption per job versus load, in the system with ON-OFFs for different values of f. We se that energy can be saved when f is small and the "off" cycle is long.



Figure 8. Theoretical and measured energy consumption per job versus load, in the system with ON-OFFs for f = 0.005. Figure 9. Composite Energy-QoS cost metric versus load in the system with ON-OFFs for f = 0.005.

Sensible Selection of a Cloud Response Time vs Load



Sensible Selection of a Cloud Response Time vs Load

Single Job Queue



Sensible Selection of a Cloud **Composite Cost Function vs Load**

Single Job Queue – A=1 B=10



Energy efficiency in wired networks

- Techniques for energy savings in wireless (sensor) networks have been very widely studied
- Wired networks have been largely neglected even though they are massive consumers of power
- In a wired packet network the problem is to:
 - Minimize total power consumption, and obviously ...
 - Respect users' QoS needs

The Network Case: Experiments











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Measurements on Feasibility Using our 46-node Laboratory Packet Network Test-Bed:

E. Gelenbe and S. Silvestri, ``Optimisation of Power Consumption in Wired Packet Networks," Proc. QShine'09, 22 (12), 717-728, LNICST, Springer Verlag, 2009.

Fig. 1. Topology of the test-bed in use



Power Measurement on Routers



Example of Measured Router Power Profile



Experiments with a Self-Aware Approach Minimise Power subject to End-to-End Delay (80ms) Constraint

[10] E. Gelenbe, ``Steps Toward Self-Aware Networks,'' Comm. ACM, 52 (7), pp. 66-75, July 2009.

[15] E. Gelenbe and T. Mahmoodi "Energy aware routing in the Cognitive Packet Network", presented at NGI/Co July 2010, submited for publication.



Measuring Avg Power Over All Routers Imperial College London



Power and Delay with EARP Energy Aware Routing Protocol



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Power Savings and QoS using EARP



Fig. 2. Scenario two: Total power consumption in the network Vs. the experiment's elapsed time.



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(b) Average length of the end-to-end path

Fig. 3. Scenario two: round trip delay and the route length of the active flows.

Can Analysis and Optimisation Help for the Network Case?

IDEA:

Build a Queueing Network with Multiple Customer Classes
- A Node is a Network Router or a Network Link
- A Class is a Flow of Packets that follow the same Path

- Add Triggers to Model Control Signals that Reroute the Normal Customer Classes and also Consume Resources

Define a Cost Function that Includes Power Consumption as A Function of Load, and also A verage Response Time
Solve using G-Network Theory
Optimise with Gradient Descent & Non-Linear Optimisation

G-networks allow product form solutions including the routing control

Rerouting controls occur infrequently (seconds) as compared to individual packet service times (1ms) and end-to-end packet travel times (10ms)

- The system attains steady-state between the control instants
- G-networks [11,12,13] with triggered customer movement and multiple classes are a convenient modelling paradigm for packet networks with controls
- Network with N queues, R routers and L links, N=R∪L
- Set of user traffic classes U
- The default routing decision of a user of class k from node i to node j is represented by the probability P(i,k,j)
- The external arrival rate of packets of class k to router r is denoted by λ(r,k)
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G-networks allow product form solutions that include the effect of re-routing Current default routing decision of a user of class k from neighbouring queues i to j is P(i,k,j)

- Control traffic class (r,k): acts at router r on traffic class k
- A control packet of class (r,k) moves from queue i to j with probability p((r,k),i,j)
- Control function Q(r,k,j) : probability that user of class k at router r is directed by the corresponding control packet of type (i,k) to link j.
- External arrival rate of control packets of class (r,k) to router i : λ⁻(i(r,k))

Traffic in the Network

- The steady state probability that a router r or a link l contains at least one packet of user class k is given by $q(r,k) = \frac{\Lambda_R(r,k)}{\mu_r + \Lambda^-(r,(r,k))}$, if $r \in \mathbb{R}$ $q(l,k) = \frac{\Lambda_L(l,k)}{\mu_l}$, if $l \in \mathbb{L}$
- The total arrival rates of user packets of class k to the routers and links are given by

$$\Lambda_{R}(r,k) = \lambda(r,k) + \sum_{l \in \mathbf{L}} q(l,k)P(l,k,r)\mu_{l}, \text{ if } r \in \mathbf{R}$$

 $\Lambda_L(l,k) = \sum_{r \in \mathbf{R}} [q(r,k)P(r,k,l)\mu_r + \Lambda^-(r,(r,k))q(r,k)Q(r,k,l)], \text{if } l \in \mathbf{L}$

Control Traffic

 The total arrival rate to router or link j of control traffic of class (i,k) is given by $\Lambda^{-}(j,(i,k)) = \lambda^{-}(j,(i,k)) + \sum_{i=1}^{n} p((i,k),l,j)c(l,(i,k))\mu_{l}, \text{if } i, j \in \mathbf{R}$ $\Lambda^{-}(j,(i,k)) = \sum p((i,k),r,j)K(r,(i,k))\mu_r, \text{if } i \in \mathbf{R}, j \in \mathbf{L}, i \neq r$ The steady-state probability that a router r contains at least one packet of class k is $c(l,(i,k)) = \frac{\sum_{r \in \mathbb{R}} p((i,k),r,l)K(r,(i,k))\mu_r}{\text{, if } l \in \mathbb{L}}$ μ_l

And for the routers

$$K(r,(i,k)) = \frac{\lambda^{-}(r,(i,k)) + \sum_{l \in \mathbf{L}} p((i,k),l,r)c(l,(i,k))\mu_l}{\mu_l}, \text{ if } r \in \mathbf{R}, r \neq i$$

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Average Queue Length

• Each user class is assumed to be handled by separate queues in routers, so the average queue length in router r is

$$N(r,k) = \frac{q(r,k)}{1 - q(r,k)}, r \in \mathbf{R}$$

• On the other hand, all packets within a link are handled in a first-come-first-serve order, so the average queue length at link / is

$$N(l) = \frac{B(l)}{1 - B(l)}, l \in \mathbf{L}$$

where

$$B(l) = \sum_{k \in \mathbf{U}} [q(l,k) + \sum_{i \in \mathbf{R}} c(l,(i,k))]$$

is the steady state probability that link / is busy Imperial College London

QoS metrics

• The relevant QoS metrics, e.g. the total average delay through the network for a packet of class k

$$T(k) = \sum_{l \in \mathbf{L}} \pi(l,k) \frac{N(l)}{\Lambda_L(l,k)} + \sum_{r \in \mathbf{R}} \pi(r,k) \frac{N(r,k)}{\Lambda_R(l,k)}, \quad \bar{T} = \sum_k T(k)$$

here
$$\pi(r,k) = \frac{\Lambda_R(r,k)}{\lambda^+(k)}, r \in \mathbf{R} \qquad \pi(l,k) = \frac{\Lambda_L(l,k)}{\lambda^+(k)}, l \in \mathbf{L}$$

are the probabilities that a packet of class k enters router r or link I respectively, and the total traffic of class k, s being the source router of this class is

Imperial College $\lambda^+(k) = \sum_{r \in \mathbb{R}} \lambda(r,k) = \lambda(s,k)$ London

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Power Consumption Model

• Routers

$$P_i = \alpha_i + g_R(\Lambda_i) + c_i \sum_{k \in \mathbf{U}} \Lambda_R^-(i, (i, k)), i \in \mathbf{R}$$

where α_i is the static router power consumption, $g_R(.)$ is an increasing function of the packet processing rate as in Figure 1 and $c_i > 0$ is a proportionality constant related to the power consumed for the processing of the rerouting control

• Links $P_i = \beta_i + g_L(\Lambda_i), i \in \mathbf{L}$

where β_i is the static power consumption when the link interface is on and $g_L(.)$ is an increasing function of the data transmission rate on the link as in Figure 2

Gradient Descent Optimisation

- The routing optimisation can be expressed as the minimization of a function that combines power consumption and (e.g.) the network average delay : Minimize $G = c \sum_{i \in N} P_i + \overline{T}$ Using the Q(i,k,j)
- We therefore need to design algorithm to obtain the parameters Q^o(i,k,j) at the operating points of the network

$$\underline{X} = [\underline{\lambda}, \underline{\lambda}^{-}, \mu, \underline{P}^{+}, p]$$

A. Gradient Descent Optimization

- Algorithm of O(|U|.|N|³) complexity [High!!]
 - Initialize the values Q(i,k,j) and choose η>0
 - Solve |U| systems of |N | non-linear equations to obtain the steady state probabilities q(i,k) from G-network theory
 - Solve |U| systems of |N | linear equations for gradient descent using G-network theory

$$\frac{\partial \mathbf{q}_k}{\partial Q(x,m,y)} = \boldsymbol{\gamma}_k^{xmy} (\mathbf{I} - \mathbf{W}_k)^{-1}$$

- Update the values of Q(i,k,j) using the nth computational step $Q_{n+1}(i,k,j) = Q_n(i,k,j) - \eta \frac{\partial G}{\partial O(i,k,j)}|_{Q(i,k,j)=Q_n(i,k,j)}$

Gradient Descent on Top of EARP



A Model for Time & Energy that is both Cyber & Physical, and E. Gelenbe Phys Rev Dec 2010

- N robots or people Search in an Unknown & Large City
- N Packets Travel in a Very-Large Network
- Search by Software Robots for Data in a Very Large Distributed Database
- Biological Agents Diffusing through a Random Medium
 until they Encounter a Docking Point
- Particles Moving in a Random Medium until they Encounter an Oppositely Charged Receptor
- Randomised Gradient Minimisation (e.g. Simulated Annealing) on Parallel Processors

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Example from Wireless Sensor Networks Event occuring at location (x,t) is reported by the Sensor Node at location (n,t+d) if $||X(n)-x|| < \varepsilon$. The node sends out a packet at t+d. The packet containing M(n,X(n),t+d) travels over multiple hops and reaches the Output Node at time t+d+T

Source of Event

 $\sqrt{2}M(n,t+d)$

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Output Node

A Packet Needs to Go From S to Destination Using Multiple Hops .. But it is Ignorant about its Path and all Kinds of Bad Things Can Happen .. Can it Still Succeed?

Source

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B

45

Destination

Yet Another Situation .. Packet Hara Kiri

I-the-Packet have already visited 6 hops I'll do hara-kiri 'coz I'm too old!!



Source

B

Destination

Some Time Later .. Packet Retransmission

The packet had visited 6 hops .. I'll drop it 'coz 'tis too old!!

Destination

6+M Time units elapsed: the packet must be lost. I'll-send it

again.

1NN

Source

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B

Network Model

- Packets go from some source S to a Destination (that may move) that is initially at distance D
- The wireless range is $\delta \ll D$, there are no collisions
- Packets can be lost in [t,t+ Δ t] with probability $\lambda\Delta$ t anywhere on the path
- There is a time-out R (in time or number of hops), modelled as being timed-out in [t,t+∆t] with probability r∆t with a subsequent retransmission delay M
- Packets may or not know the direction they need to go – we do not nail down the routing scheme with any specific assumptions
- We avoid assumptions about the geography of nodes in m-dimensions, and assume temporal and spatial homogeneity and temporal and spatial independence

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Simulations of Average Travel Time vs Constant Time-Out δ=1, D=10, M=20, No Loss Perfect Ignorance: b=0, c=1



Imp

Diffusion Model

- Do not consider the detailed topology of nodes,

- Assume homogeneity with respect to the distance to destination, and over time,

- Represent motion as a continuous process, for packets it would be a continuous approximation of discrete motion,

- Allow for loss (of packets) or destruction of the robotic searcher, or inactivation of the biological agent

- Include a time-out for the source to re-send the packet

- After each Time-Out, the sender waits M time units and then Imperial College packet under identical statistical conditions - The distance of the searcher with respect to the destination at time t is X(t); it is homogeneous with respect to position and time

- Motion of the searcher is characterised by parameters b and

- The drift $b = E[X(t + \Delta t) - X(t)|X=x] / \Delta t$ - The instantaneous variance $c = E[(X(t + \Delta t) - X(t) - b\Delta t)^2 | X = x] / (\Delta t)^2$

C

- Loss (of packets), destruction of the robotic searcher, inactivation of the biological agent, represented by $\lambda \Delta t$

- Time-out is represented by $r\Delta t$, and after each Time-out, the sender waits M (on average $1/\mu$) time units and then resends the packet which then travels under iid statistical Cullege 09/09/2013

N independent searchers: find average time for the first one to get there



$$\begin{aligned} \frac{\partial f_i}{\partial t} &= -b \frac{\partial f_i}{\partial x_i} + \frac{1}{2} c \frac{\partial^2 f_i}{\partial x_i^2} - a_i f_i + [\mu W_i(t) + P_i(t)] \delta(x_i - D) \\ \frac{dP_i(t)}{dt} &= -P_i(t) + \sum_{i=1}^{N} \lim_{x_i \to 0^+} [-bf_i + \frac{1}{2} c \frac{\partial f_i}{\partial x_i}] \\ \frac{dL_i(t)}{dt} &= \lambda \int_{0^+}^{\infty} f_i dx_i - (r + a_i) L_i(t) \\ \frac{dW_i(t)}{dt} &= r \int_{0^+}^{\infty} f_i dx_i + rL_i(t) - (\mu + a_i) W_i(t) \\ a_j &= -\sum_{i=1, i \neq j}^{N} \lim_{x_i \to 0^+} [-bf_i + \frac{1}{2} c \frac{\partial f_i}{\partial x_i}], \\ P_i(t) + L_i(t) + W_i(t) + \int_{0^+}^{\infty} f_i dx_i = 1; \quad \lim_{x \to 0^+} f = 0. \\ \mathbf{E}[\mathbf{T}^*] &= \mathbf{P}_i^{-1} - 1 \text{ obtained from the stationary solution} \end{aligned}$$

54

infinity

P(†)

 $f_i(z) = A[e^{u_1 z} - e^{u_2 z}], 0 \le z \le D$ $f_i(z) = A[e^{(u_1 - u_2)D} - 1]e^{u_2 z}, z \ge D$ $u_{1,2} = \frac{b \pm \sqrt{+2c(\lambda + r + a)}}{2}$ $a_{i} = \sum_{j=1, i \neq j}^{N} \lim_{z_{j} \to 0} [bf_{j}(z_{j}) + \frac{1}{2}c \frac{\partial^{2} f_{j}(z_{j})}{\partial z_{j}^{2}}]$ P(†) infinity Imperial College 55 London

Expected Travel Time to Destination for N Searchers with initial Distance D

 $T^* = \inf \{T_1, ..., T_N\}$

- Drift b ≤ 0 or b>0, Second Moment Param.
 c≥0
- Avg Time-Out R=1/r, M=1/μ, then we derive:

$$E[T \mid D] = \frac{1}{N} \left[e^{-2D(\frac{\lambda + r + a}{b - \sqrt{b^2 + 2c(\lambda + r + a)}})} - 1 \right] \left[\frac{\mu + r + a}{(r + a)\mu + a} \right]$$

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Effective Travel Time & Energy

 $T^* = \inf \{T_1, ..., T_N\}$ • E[$\tau_{eff} | D$] = [1+E[T* | D]]. P[searcher is moving] • J(N | D) = N.E[$\tau_{eff} | D$]

$$J(N \mid D) = [e^{-2D(\frac{\lambda + r + a}{b - \sqrt{b^2 + 2c(\lambda + r + a)}})} -1][\frac{1}{\lambda + r + a}]$$

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Comparing Theory with Simulation for N=1



Average Travel Time vs Time-Out and Different N and Loss Rates



Locus of Average Time and Energy vs Time-Out



Locus of Average Time and Energy vs Time-Out with Different Distances



Single packet travel delay in a wireless network with imperfect routing and packet losses

- E. Gelenbe "A Diffusion model for packet travel time in a random multi-hop medium", ACM Trans. on Sensor Networks, Vol. 3 (2), p. 111, 2007
- N Packets or Searchers sent simultaneously in a homogenous environment:
- E. Gelenbe "Search in unknown random environments", Physical Review E82: 061112 (2010), Dec. 7, 2010.



Results ACM MAMA 2011 Omer Abdelrahman & Erol Gelenbe Single packet travel delay in a wireless network with non-homogenous parameters, imperfect routing and packet losses

Large Network with Non-Homogenous
 Coverage

 Modeling an Attacking Packet in the presence of Defense Near the Target (Destination) Node

→ Phase Transition Effect

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Non-HomogenousCaseOriginalDiscretized

 $\frac{1}{2} \frac{\partial^2 [c(z)f(z,t)]}{\partial [b(z)f(z,t)]} = \frac{\partial [b(z)f(z,t)]}{\partial [b(z)f(z,t)]}$ $\partial f(z,t)$ ∂t $-(\lambda(z) + r)f(z,t) + [P(t) + \mu W(t)]\delta(z - D)$ $\frac{dL(t)}{dt} = -rL(t) + \int_{0}^{\infty} \lambda(z)f(z,t)dz$ $\frac{dW(t)}{dt} = -\mu W(t) + r[L(t) + \int_0^\infty f(z,t)dz]$ $\frac{dP(t)}{dt} = -P(t) + \lim_{z \to 0^+} \left[\frac{1}{2} \frac{\partial [c(z)f(z,t)]}{\partial z} - b(z)f(z,t)\right]$ $1 = P(t) + W(t) + L(t) + \int_{-\infty}^{\infty} f(z,t)dz$

$$0 = \frac{c_k}{2} \frac{d^2 f_k(z)}{dz^2} - b_k \frac{df_k(z)}{dz} - (\lambda_k + r)f_k(z) \qquad (1)$$

while the equation for the segment where the source is located is:

$$-[P + \mu W]\delta(z - D) = \frac{c_n}{2}\frac{d^2f_n(z)}{dz^2} - b_n\frac{df_n(z)}{dz} - (\lambda_n + r)f_n(z) \quad (2)$$

We will also have:

$$rL = \sum_{k=1}^{m} \lambda_k \int_{Z_{k-1}}^{Z_k} f_k(z) dz$$
 (3)

$$\mu W = r[L + \sum_{k=1}^{m} \int_{Z_{k-1}}^{Z_k} f_k(z) dz]$$
(4)

$$P = \lim_{z \to 0^+} \left[\frac{c_1}{2} \frac{df_1(z)}{dz} - b_1 f_1(z) \right]$$
(5)

and the normalization condition:

$$1 = P + W + L + \sum_{k=1}^{m} \int_{Z_{k-1}}^{Z_k} f_k(z) dz \qquad (6)$$

Discretized Segments

$$E[T] = \left(\frac{1}{r} + \frac{1}{\mu}\right) \times \left[\sqrt{\frac{b_n^2 + 2c_n(\lambda_n + r)}{b_1^2 + 2c_1(\lambda_1 + r)}} \frac{\overline{A}_n \overline{G}_n e^{u_n S_n} - \overline{B}_n \overline{F}_n e^{v_n S_n}}{\overline{G}_n e^{u_n(Z_n - D)} + \overline{F}_n e^{v_n(Z_n - D)}} - 1\right]$$

$$(7)$$

where the remaining parameters are computed as follows. Define:

$$\alpha_k^- = \frac{c_k u_k - c_{k-1} v_{k-1}}{c_k (u_k - v_k)}, \quad \beta_k^- = \frac{c_k u_k - c_{k-1} u_{k-1}}{c_k (u_k - v_k)}$$
$$\alpha_k^+ = \frac{c_k u_k - c_{k+1} v_{k+1}}{c_k (u_k - v_k)}, \quad \beta_k^+ = \frac{c_k u_k - c_{k+1} u_{k+1}}{c_k (u_k - v_k)}$$
(8)

Then set $\overline{A}_1 = 1$ and $\overline{B}_1 = -1$ and for $2 \leq k \leq n$ compute:

$$\begin{bmatrix} \overline{A}_{k} \\ \overline{B}_{k} \end{bmatrix} = \begin{bmatrix} \alpha_{k}^{-} & \beta_{k}^{-} \\ 1 - \alpha_{k}^{-} & 1 - \beta_{k}^{-} \end{bmatrix} \begin{bmatrix} e^{u_{k-1}S_{k-1}} & 0 \\ 0 & e^{u_{k-1}S_{k-1}} \end{bmatrix} \begin{bmatrix} \overline{A}_{k-1} \\ \overline{B}_{k-1} \end{bmatrix}$$
(9)

Then set $\overline{F}_m = 0$ and $\overline{G}_m = e^{v_m Z_m}$, and start another computation at k = m - 1 for $n \leq k \leq m - 1$ with:

$$\begin{bmatrix} \overline{F}_{k} \\ \overline{G}_{k} \end{bmatrix} = \begin{bmatrix} \alpha_{k}^{+} & \beta_{k}^{+} \\ 1 - \alpha_{k}^{+} & 1 - \beta_{k}^{+} \end{bmatrix} \begin{bmatrix} e^{-u_{k+1}S_{k+1}} & 0 \\ 0 & e^{-v_{k+1}S_{k+1}} \end{bmatrix} \begin{bmatrix} \overline{F}_{k+1} \\ \overline{G}_{k+1} \end{bmatrix}$$

Discretized Segments

Remark 1 With n being the index of the discretisation segment that includes the source node at D, it is interesting to see that E[T] only depends on a set of parameters that are computed for values of k = 1, k = n, and on two sets of algebraic iterations between k = 1 and k = n and k = mdown to k = n.

Remark 2 When the source node is in the pen-ultimate segment we have m = n, and:

$$E[T] = \frac{r+\mu}{r\mu} \left[\sqrt{\frac{b_n^2 + 2c_n(\lambda_n + r)}{b_1^2 + 2c_1(\lambda_1 + r)}} \overline{A}_n e^{u_n(D-Z_{n-1})} - 1 \right]$$
(20)

For a homogenous medium m = n = 1 and:

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$$E[T] = \left(\frac{1}{r} + \frac{1}{\mu}\right) \left[e^{u_1 D} - 1\right]$$

Increased Drop Rate Near the Destination Makes it Harder to Reach the Destination



Protected Area of Size S Around Destination with Intrusion Detection and Drops



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68

Protected Destination with Perfect Routers b= -1

Now let us introduce a non-homogenous packet drop effect by choosing an integer n to create an acceleration in the packet drop effect and let $S_i = D/(n-1)$ so that:

$$E[T] = \frac{r+\mu}{r\mu} \left[e^{rD} \ e^{D\frac{\sum_{i=1}^{n-1}\lambda_i}{n-1}} - 1 \right]$$
(24)

which yields the following result.

Result 4 If $\lim_{n\to\infty} \frac{\sum_{i=1}^{n-1} \lambda_i}{n-1} = +\infty$ then the packet will never reach the destination node. Otherwise it will reach it in a time which is finite on average, and with probability one. The Figure 2 illustrates **Result 4** by showing that even with a small excess, represented by a > 1, above the o(n)rate of increase for the loss rate λ_k the attacking packet's progress will be indefinitely impeded by the drops, despite the subsequent time-outs

Increased Drop Rate Near the Destination Makes it Hard to Reach the Destination



Energy Consumption: Protected Area of Size S Around Destination with Intrusion Detection and Drops



Increased Drop Rate Near the Destination: Phase Transition Effect for Protection



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72
What if the Energy Infrastructure wer Designed like the Internet?

- Energy: the limited resource of the 21st Century
- Needed: Information Age approach to the Machine Age infrastructure
- Lower cost, more incremental deployment, suitable for developing economies
- Enhanced reliability and resilience to wide-area outages, such as after natural disasters
- Packetized Energy?: Discrete units of energy locally generated, stored, and forwarded to where it is needed; enabling a market for energy exchange

New Energy Systems

- A scalable energy network ?
 - Address inefficiencies at all levels of electrical energy distribution
 - Address energy generation and storage
 - IPS and PowerComm Interface
 - Energy sharing marketplace at small, medium, large scale
- Energy Supply on Demand
- Imagine some Test-beds: Smart buildings, datacenters

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